

Problem 1. Calculate derivatives / higher-order derivatives.

1. $(2 \sin(x^3 + x) + x)' =$

2. $((\sin^4 x + x - 1)^{100})' =$

3. $(\cos(\frac{\sin x}{x^3 - 1}))' =$

4. $(\sqrt{x^2 + 1})''' =$

5. $(\sin(x^2))''' =$

6. $(\cos(2x))^{(31)} =$

Problem 2. Find the tangent line to the graph of $x^3 + xy - y^2 - y^4 = -2$ at $(1, -1)$.

Problem 3. Find $\frac{dy}{dx}$, $\frac{d^2y}{dx^2}$ for the following implicit functions $y(x)$.

$$(1) \quad x^2 + xy + y^3 = 1$$

$$(2) \quad 2x^4 + xy^2 + \cos(y^2) = 1$$