

**Each group only needs to submit ONE file containing your solutions!**

**Problem 1.** Consider a damped harmonic oscillator

$$h'' + 2\eta h' + 25h = 0, \quad h(0) = 1, \quad h'(0) = 0$$

- (1) For the situations  $\eta_1 = 4$ ,  $\eta_2 = 5$ ,  $\eta_3 = 6$ , solve the ODE. Which classes (under damped, over damped, critically damped) do they belong to?
- (2) For the three solutions in (1), which one decays fastest to zero as  $t \rightarrow \infty$ ?

**Problem 2.** Consider a damped harmonic oscillator

$$h'' + 3h' + 2h = 0, \quad h(0) = 1, \quad h'(0) = x$$

where  $x$  is a real number. For what values of  $x$ , the solution  $h(t)$  is a monotone function for all  $t \geq 0$ ?